

## 5. CORRELATION



### Let's Study

- Concept of Correlation
- Methods of computing correlation
- Properties of Covariance
- Karl Pearson's coefficient of correlation
- Scatter diagram
- Interpretation



### Let's Observe...

So far, we have studied the statistical methods used for analysis of data involving only one variable. There are situations where two variables are involved

For example consider following data,

- (i) Demand and Price of a certain commodity over a specified period of time.
- (ii) Weight of a person and Blood Pressure of the person.
- (iii) Quantity of water and crop yield.
- (iv) Sales of cosmetics and advertisements
- (v) Monthly income and expenditure of a family.

A set of observations made on two variables is called Bivariate Data. The two variables are denoted by X and Y respectively. Then observations on two variables X and Y can be represented by  $n$  ordered pairs  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n), \dots$ . The pair  $(x_i, y_i)$ , values of the variables for  $i^{\text{th}}$  observation. For example X denotes demand of the commodity and Y denotes price of the commodity then  $x_i$  denotes demand of  $i^{\text{th}}$  commodity and  $y_i$  denotes price of  $i^{\text{th}}$  commodity.



### Let's Learn

#### 5.1 Concept of Correlation

In a bivariate data, we may be interested in finding if there is any relationship or association between the two variables. "A correlation is a measure of association or relation". If we observe in the bivariate data the changes in one variable are accompanied by changes in the other variable then the two variables are said to be correlated. In this case we say that there is a correlation between two underlying variables.

**For example,**

- i) Intelligence Quotient (IQ) and marks of a student.
- ii) Demand and price of a commodity.



### Let's discuss:

#### 5.2 Covariance:-

Covariance is a measure of joint variation between the two variables. If  $(x_1, y_1), (x_2, y_2), (x_n, y_n)$  are  $n$  ordered pairs of values of  $x$  and  $y$ , then covariance between X and Y is defined by

$$\text{cov}(x, y) = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}),$$

$$\text{where } \bar{x} = \frac{\sum x_i}{n} \text{ and } \bar{y} = \frac{\sum y_i}{n}.$$

The above formula can be simplified as follows :

$$\begin{aligned} \text{cov}(x, y) &= \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) \\ &= \frac{1}{n} \sum_{i=1}^n (x_i y_i - x_i \bar{y} - \bar{x} y_i + \bar{x} \bar{y}) \end{aligned}$$

$$\begin{aligned}
&= \frac{1}{n} \left[ \sum_{i=1}^n x_i y_i - \bar{y} \sum_{i=1}^n x_i - \bar{x} \sum_{i=1}^n y_i + \sum_{i=1}^n \bar{x} \bar{y} \right] \\
&= \frac{1}{n} \left[ \sum_{i=1}^n x_i y_i \right] - [\bar{y} \bar{x} - \bar{x} \bar{y} + \bar{x} \bar{y}] \\
&= \frac{1}{n} \sum_{i=1}^n x_i y_i - \bar{x} \bar{y}
\end{aligned}$$

This formula is used in practice.

### 5.3 Properties of covariance:

- (i)  $\text{Cov}(X, Y) = \text{Cov}(Y, X)$
- (ii)  $\text{Cov}(X, C) = 0$  where  $C$  is a constant
- (iii) Covariance may be positive, negative or zero.
- (iv)  $\text{Cov}(X, X) = \text{Var}(X)$
- (v) Covariance is invariant under change of origin but is affected by change of scale.

That is if  $U = \frac{x-a}{h}$  and  $V = \frac{y-b}{k}$ , where

$a, b, h, k$  are constants and  $h \neq 0, k \neq 0$  then,

$$\text{Cov}(U, V) = \frac{1}{hk} \text{Cov}(X, Y)$$

$$\text{Cov}(X, Y) = hk \text{Cov}(U, V)$$

Note that these are standard deviations of  $X$  and  $Y$  respectively.

$$\sigma_x = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2} = \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2 - \bar{x}^2}$$

$$\sigma_y = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2} = \sqrt{\frac{1}{n} \sum_{i=1}^n y_i^2 - \bar{y}^2}$$

Compare and understand the difference between variance and co-variance.

### 5.4 Correlation coefficient:-

Karl Pearson (1867-1936) developed a measure for the degree of relation between two variables. This measure is called correlation coefficient.

Correlation coefficient between two random variables  $X$  and  $Y$  denoted by  $r_{xy}$  or  $r(x, y)$  is defined by

$$r_{xy} = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$$

### Properties of correlation coefficient $r(x, y)$ :-

- (i)  $r_{xy} = r_{yx}$  (order of variable is not important).
- (ii) Change of origin and scale :

Correlation coefficient ( $r$ ) does not change its magnitude under the change of origin and scale.

- (iii) But if one of the change of scale has Negative sign then correlation coefficient becomes negative.

$$\text{Correlation} \left( \frac{x-a}{h}, \frac{y-b}{k} \right) = \text{Correlation}(x, y)$$

if  $h, k$  has same algebraic sign  $r_{uv} = r_{xy}$  also  $h, k \neq 0$ ,  $r_{uv} = -r_{xy}$  if  $h, k$  have opposite algebraic sign

- (iv)  $\text{Correlation}(x, x) = 1$ .

- (v)  $r$  lies between  $-1$  and  $1$  that is  $-1 \leq r \leq 1$

### 5.5 Scatter Diagram:-

A scatter diagram is a graphical method of presenting bivariate data (grouped and ungrouped).

Correlation can be observed in a scatter diagram.

Following are examples of different situations given different types of scatter diagrams.

#### (I) a) Perfect positive correlation:-

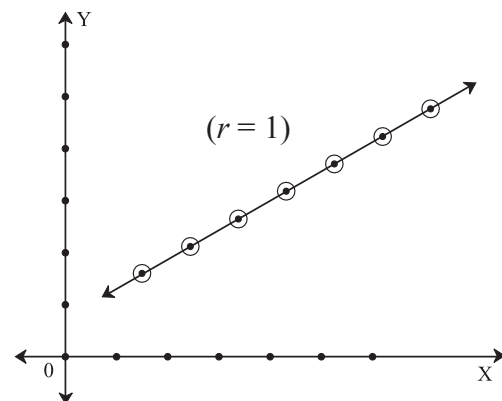
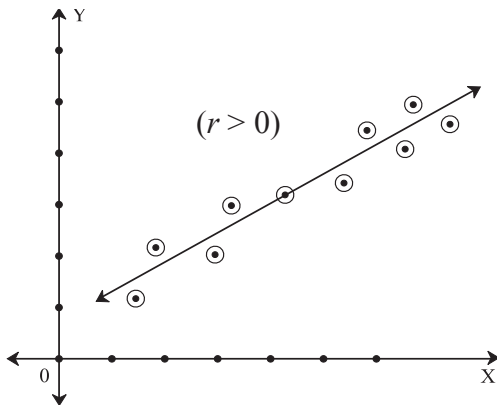


Fig 5.1

If the points are rising from left to right in a straight line then scatter diagram indicates a perfect positive correlation.

**b) Positive correlation with high degree:-**

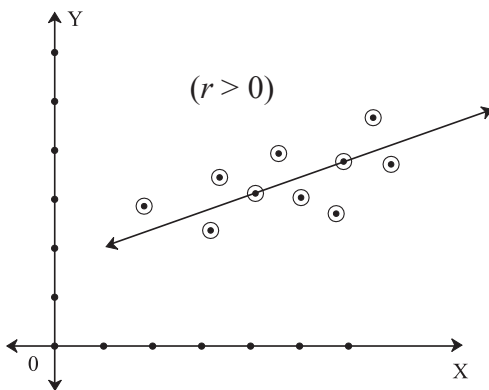
If the band is rising from left to right then it indicates positive correlation. If the width of the band is smaller, then the correlation is of high degree.



**Fig 5.2**

**c) Positive correlation with low degree:-**

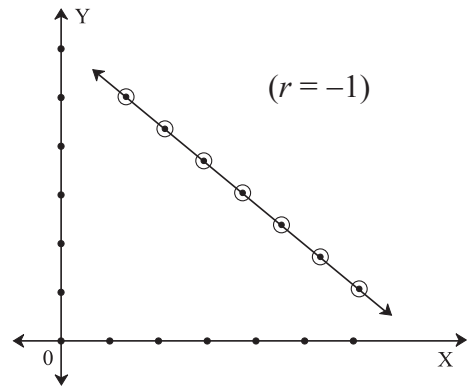
If the band is rising from left to right then it indicates positive correlation. If the width of the band is bigger, then the correlation is of low degree.



**Fig 5.3**

**(II) a) Perfect negative correlation:-**

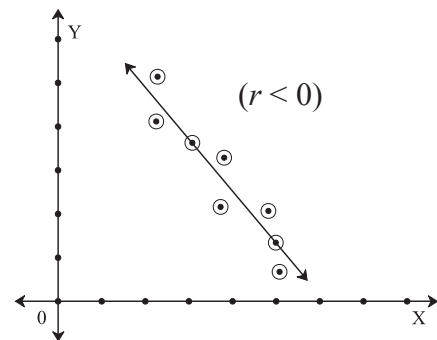
If the points are falling from left to right in a straight line then scatter diagram indicates a perfect negative correlation.



**Fig 5.4**

**b) Negative correlation with high degree:-**

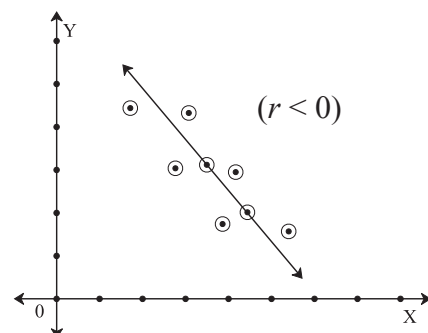
If the band is falling down from left to right it indicates negative correlation. If the width of the band is smaller, then the correlation is of high degree.



**Fig 5.5**

**c) Negative correlation with low degree:-**

If the band is falling down from left to right it indicates negative correlation. If the width of the band is bigger then the correlation is of low degree.



**Fig 5.6**

### (III) No correlation (Zero correlation):-

In this case no trend line is observed.

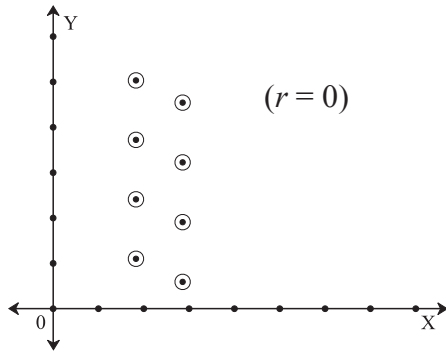


Fig 5.7

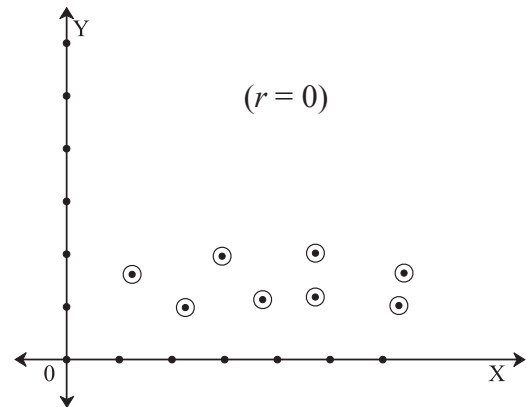


Fig 5.10

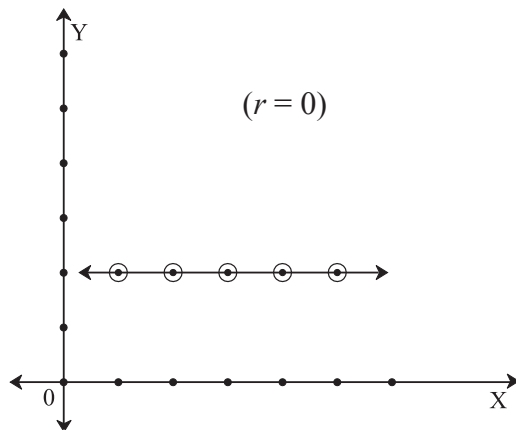


Fig 5.8

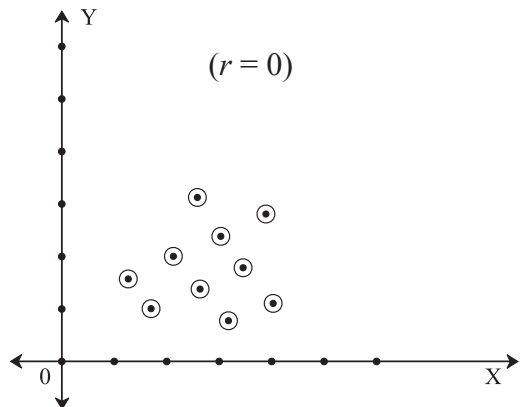


Fig 5.11

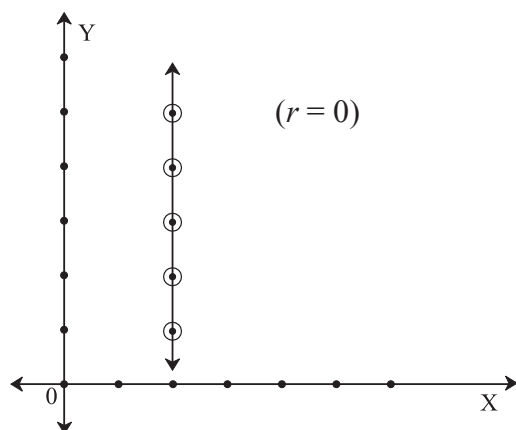


Fig 5.9

### 5.6 Interpretation of value of correlation coefficient:-

If  $r > 0$ , the correlation is positive.

If  $r < 0$ , the correlation is negative.

If  $r = 0$ , there is no correlation.

If  $r > 0.8$ , there is high positive correlation.

If  $0.3 < r < 0.8$ , there is moderate positive correlation.

If  $|r| < 0.3$ , the correlation is insignificant or poor.

If  $r = 1$ , the correlation is perfect positive.

If  $r = -1$ , the correlation is perfect negative.

### Alternative formula of correlation coefficient:-

$$(i) \quad r = \frac{\Sigma(x - \bar{x})(y - \bar{y})}{\sqrt{\Sigma(x - \bar{x})^2} \sqrt{\Sigma(y - \bar{y})^2}}$$

when  $\bar{x}$ ,  $\bar{y}$  are integers & small nos.

$$(ii) \quad r = \frac{n\Sigma xy - \Sigma x \Sigma y}{\sqrt{n\Sigma x^2 - (\Sigma x)^2} \times \sqrt{n\Sigma y^2 - (\Sigma y)^2}}$$

when  $\bar{x}$ ,  $\bar{y}$  are decimals  $\Sigma x$ ,  $\Sigma y$  are comparatively small nos.

(iii) For change of origin & scale

$$r_{uv} = \frac{n\Sigma uv - \Sigma u \Sigma v}{\sqrt{n\Sigma u^2 - (\Sigma u)^2} \times \sqrt{n\Sigma v^2 - (\Sigma v)^2}}$$

### SOLVED EXAMPLES

1) A train travelled between two stations and distance and time were recorded as below,

|              |    |     |     |     |     |
|--------------|----|-----|-----|-----|-----|
| Distance(km) | 80 | 120 | 160 | 200 | 240 |
| Time(Hr)     | 2  | 3   | 4   | 5   | 6   |

Draw scatter diagram and identify the type of correlation.

**Solution:** Here we take distance on X- axis and Time on Y- axis and plot the points as below,

**Graph:-**

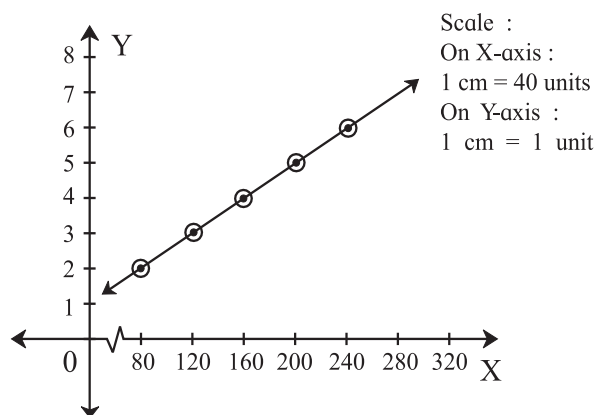


Fig 5.12

Since all the points lie on the straight line rising from left to right, there is perfect positive correlation between distance and time for the train.

2) Draw scatter diagram for the following data and identify the type of correlation.

|                         |   |   |   |   |   |   |    |
|-------------------------|---|---|---|---|---|---|----|
| Capital (in crores Rs.) | 2 | 3 | 4 | 5 | 6 | 8 | 9  |
| Profit (in lakh Rs.)    | 6 | 5 | 7 | 7 | 8 | 9 | 10 |

**Solution:** Here we take capital on X- axis and profit on Y- axis and plot the points as below,

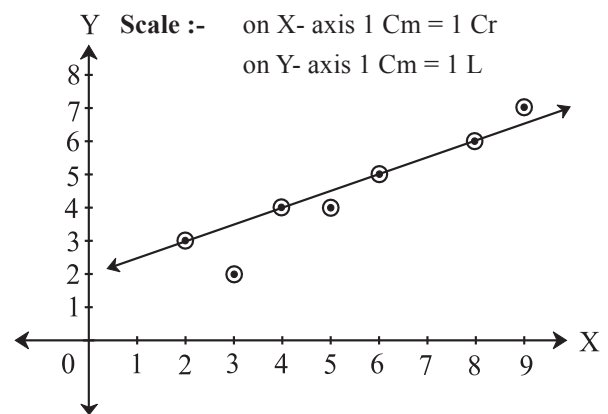


Fig 5.13

We get a band of points rising left to right. This indicates the positive correlation between capital and profit.

3) Compute correlation coefficient for the following data,

$$n = 100, \bar{x} = 62, \bar{y} = 53, \sigma_x = 10, \sigma_y = 12, \Sigma(x_i - \bar{x})(y_i - \bar{y}) = 8000.$$

**Solution:** Given that  $n = 100, \bar{x} = 62, \bar{y} = 53, \sigma_x = 10, \sigma_y = 12,$   
 $\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 8000.$

For finding correlation coefficient, we require  $\text{cov}(x, y)$  and  $\sigma_x$  and  $\sigma_y$

$$\begin{aligned}\text{cov}(x,y) &= \frac{1}{n} \sum (x_i - \bar{x})(y_i - \bar{y}) \\ &= \frac{8000}{100} \\ &= 80. \\ r &= \frac{\text{cov}(x,y)}{\sigma_x \sigma_y} = \frac{80}{10 \times 12} = 0.67\end{aligned}$$

- 4) Find correlation coefficient between  $x$  and  $y$  for the following data and interpret it.

|   |    |    |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|----|----|
| x | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| y | 12 | 11 | 13 | 15 | 14 | 17 | 16 | 19 | 18 |

$$(\sqrt{666} = 25.80)$$

**Solution:** For finding correlation coefficient, we require  $\text{cov}(x,y)$  and  $x$  and  $y$ . We construct the following table,

| $x_i$       | $y_i$ | $x_i^2$ | $y_i^2$ | $x_i y_i$ |
|-------------|-------|---------|---------|-----------|
| 1           | 12    | 1       | 144     | 12        |
| 2           | 11    | 4       | 121     | 22        |
| 3           | 13    | 9       | 169     | 39        |
| 4           | 15    | 16      | 225     | 60        |
| 5           | 14    | 25      | 196     | 70        |
| 6           | 17    | 36      | 289     | 102       |
| 7           | 16    | 49      | 256     | 112       |
| 8           | 19    | 64      | 361     | 152       |
| 9           | 18    | 81      | 324     | 162       |
| Total<br>45 | 135   | 285     | 2085    | 731       |

**Table 5.1**

From table we have,

$$\sum x_i = 45, \sum y_i = 135, \sum x_i^2 = 285, \sum y_i^2 = 2085, \sum x_i y_i = 731.$$

$$\therefore \bar{x} = \frac{\sum x_i}{n} = \frac{45}{9} = 5, \bar{y} = \frac{\sum y_i}{n} = \frac{135}{9} = 15.$$

$$\begin{aligned}\text{cov}(x,y) &= \frac{1}{n} \sum x_i y_i - \bar{x} \bar{y} = \frac{731}{9} - (5)(15) \\ &= 81.22 - 75 = 6.22.\end{aligned}$$

$$\sigma_x = \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2 - (\bar{x})^2} = \sqrt{\frac{285}{9} - 5^2}$$

$$= \sqrt{31.66 - 25} = \sqrt{6.66} = 2.580$$

$$\sigma_y = \sqrt{\frac{1}{n} \sum_{i=1}^n y_i^2 - (\bar{y})^2} = \sqrt{\frac{2085}{9} - 15^2}$$

$$= \sqrt{231.66 - 225} = \sqrt{6.66} = 2.58$$

$$r_{xy} = \frac{\text{cov}(x,y)}{\sigma_x \sigma_y} = \frac{6.22}{\sqrt{6.66} \sqrt{6.66}} = \frac{6.22}{6.66} = 0.93$$

There is high degree positive correlation between  $x$  and  $y$ .

- 5) Calculate correlation coefficient from the following data,

$$n = 10, \sum x_i = 140, \sum y_i = 150, \sum (x_i - 10)^2 = 180, \sum (y_i - 15)^2 = 500, \text{ and}$$

$$\sum (x_i - 10)(y_i - 15) = 60.$$

**Solution:** We are given that  $\sum x_i = 140, \sum y_i = 150, \sum (x_i - 10)^2 = 180, \sum (y_i - 15)^2 = 500$ , and  $\sum (x_i - 10)(y_i - 15) = 60$ .

Let us define  $u_i = x_i - 10$  and  $v_i = y_i - 15$ , then we have,

$$\begin{aligned}\sum u_i &= \sum (x_i - 10) = \sum x_i - \sum 10 = \sum x_i - 10n \\ &= 140 - 10 \times 10 = 40.\end{aligned}$$

$$\begin{aligned}\sum v_i &= \sum (y_i - 15) = \sum y_i - \sum 15 = \sum y_i - 15n \\ &= 150 - 150 = 0.\end{aligned}$$

$$\sum u_i^2 = \sum (x_i - 10)^2 = 180.$$

$$\sum v_i^2 = \sum (y_i - 15)^2 = 500.$$

$$\sum u_i v_i = \sum (x_i - 10)(y_i - 15) = 60.$$

$$\bar{u} = \frac{\sum u_i}{n} = \frac{40}{10} = 4, \bar{v} = \frac{\sum v_i}{n} = \frac{0}{10} = 0.$$

$$\sigma_u = \sqrt{\frac{1}{n} \sum_{i=1}^n u_i^2 - \bar{u}^2} = \sqrt{\frac{180}{10} - 4^2}$$

$$= \sqrt{18 - 16} = \sqrt{2}$$

$$\sigma_v = \sqrt{\frac{1}{n} \sum_{i=1}^n v_i^2 - \bar{v}^2} = \sqrt{\frac{500}{10} - 0^2}$$

$$= \sqrt{50-0} = \sqrt{50}$$

$$\therefore \text{cov}(u,v) = \frac{1}{n} \sum u_i v_i - \bar{u} \bar{v} = \frac{60}{10} - (4)(0) = 6$$

$$r_{uv} = \frac{\text{cov}(u,v)}{\sigma_u \sigma_v} = \frac{6}{\sqrt{2} \sqrt{50}} = 0.6$$

$$\text{But } r_{xy} = r_{uv} = 0.6.$$

- 6) Find correlation coefficient between  $x$  and  $y$  for the following data

$$n = 25, \sum x_i = 75, \sum y_i = 100, \sum x_i^2 = 250, \sum y_i^2 = 500, \sum x_i y_i = 325.$$

Solution- We are given that,  $n = 25, \sum x_i = 75, \sum y_i = 100, \sum x_i^2 = 250, \sum y_i^2 = 500, \sum x_i y_i = 325.$

$$\therefore \bar{x} = \frac{\sum x_i}{n} = \frac{75}{25} = 3. \quad \bar{y} = \frac{\sum y_i}{n} = \frac{100}{25} = 4.$$

$$\sigma_x = \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2 - (\bar{x})^2} = \sqrt{\frac{250}{25} - 3^2}$$

$$= \sqrt{10-9} = 1$$

$$\sigma_y = \sqrt{\frac{1}{n} \sum_{i=1}^n y_i^2 - (\bar{y})^2} = \sqrt{\frac{500}{25} - 4^2}$$

$$= \sqrt{20-16} = \sqrt{4} = 2$$

$$\therefore \text{cov}(x,y) = \frac{1}{n} \sum x_i y_i - \bar{x} \bar{y} = \frac{325}{25} - (3)(4)$$

$$= 13 - 12 = 1$$

$$r_{xy} = \frac{\text{cov}(x,y)}{\sigma_x \sigma_y} = \frac{1}{2} = 0.5$$

- 7) Calculate correlation coefficient between age of husbands and age of wives.

|                 |    |    |    |    |    |    |    |    |    |    |
|-----------------|----|----|----|----|----|----|----|----|----|----|
| Age of husbands | 23 | 27 | 28 | 29 | 30 | 31 | 33 | 35 | 36 | 39 |
| Age of wives    | 18 | 22 | 23 | 24 | 25 | 26 | 28 | 30 | 31 | 34 |

**Solution:** Here the change of origin and scale property can be used to find the correlation coefficient. We construct the table as below,

| $x_i$   | $y_i$ | $u_i = x_i - 31$ | $v_i = y_i - 25$ | $u_i^2$ | $v_i^2$ | $u_i v_i$ |
|---------|-------|------------------|------------------|---------|---------|-----------|
| 23      | 18    | -8               | -7               | 64      | 49      | 56        |
| 27      | 22    | -4               | -3               | 16      | 9       | 12        |
| 28      | 23    | -3               | -2               | 9       | 4       | 6         |
| 29      | 24    | -2               | -1               | 4       | 1       | 2         |
| 30      | 25    | -1               | 0                | 1       | 0       | 0         |
| 31      | 26    | 0                | 1                | 0       | 1       | 0         |
| 33      | 28    | 2                | 3                | 4       | 9       | 6         |
| 35      | 30    | 4                | 5                | 16      | 25      | 20        |
| 36      | 31    | 5                | 6                | 25      | 36      | 30        |
| 39      | 34    | 8                | 9                | 64      | 81      | 72        |
| Total - | -     | 1                | 11               | 203     | 215     | 204       |

**Table 5.2**

From table we have,

$$\sum u_i = 1, \quad \sum v_i = 11, \quad \sum u_i^2 = 203, \quad \sum v_i^2 = 215,$$

$$\sum u_i v_i = 204.$$

$$\bar{u} = \frac{\sum u_i}{n} = \frac{1}{10} = 0.1. \quad \bar{v} = \frac{\sum v_i}{n} = \frac{11}{10} = 1.1.$$

$$\therefore \text{cov}(u,v) = \frac{1}{n} \sum u_i v_i - \bar{u} \bar{v}$$

$$= \frac{204}{10} - (0.1)(1.1) = 20.4 - 0.11 = 20.29$$

$$\sigma_x = \sqrt{\frac{1}{n} \sum_{i=1}^n u_i^2 - \bar{u}^2} = \sqrt{\frac{203}{10} - 0.1^2}$$

$$= \sqrt{20.3 - 0.01} = \sqrt{20.29}$$

$$\sigma_y = \sqrt{\frac{1}{n} \sum_{i=1}^n v_i^2 - \bar{v}^2} = \sqrt{\frac{215}{10} - 1.1^2}$$

$$= \sqrt{21.5 - 1.21} = \sqrt{20.29}$$

$$r_{uv} = \frac{\text{cov}(x,y)}{\sigma_x \sigma_y} = \frac{20.29}{\sqrt{20.29} \sqrt{20.29}} = 1$$

$$\text{But } r_{xy} = r_{uv} = 1$$

### EXERCISE 5.1

- 1) Draw scatter diagram for the data given below and interpret it.

|   |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|
| x | 10 | 20 | 30 | 40 | 50 | 60 | 70 |
| y | 32 | 20 | 24 | 36 | 40 | 28 | 38 |

- 2) For the following data of marks of 7 students in Physics ( $x$ ) and Mathematics ( $y$ ), draw scatter diagram and state the type of correlation.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| x | 8 | 6 | 2 | 4 | 7 | 8 | 9 |
| y | 6 | 5 | 1 | 4 | 4 | 7 | 8 |

- 3) Draw scatter diagram for the data given below. Is there any correlation between Aptitude score and Grade points?

|                |     |     |     |     |     |     |
|----------------|-----|-----|-----|-----|-----|-----|
| Aptitude score | 40  | 50  | 55  | 60  | 70  | 80  |
| Grade points   | 1.8 | 3.8 | 2.8 | 1.7 | 2.8 | 3.2 |

- 4) Find correlation coefficient between  $x$  and  $y$  series for the following data  
 $n = 15$ ,  $\bar{x} = 25$ ,  $\bar{y} = 18$ ,  $\sigma_x = 3.01$ ,  $\sigma_y = 3.03$ ,

$$\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 122.$$

- 5) The correlation coefficient between two variables  $x$  and  $y$  is 0.48. The covariance is 36 and the variance of  $x$  is 16. Find the standard deviation of  $y$ .
- 6) In the following data one of the value of  $y$  is missing. Arithmetic means of  $x$  and  $y$  series are 6 and 8 respectively. ( $\sqrt{2} = 1.4142$ )

|   |   |    |    |   |   |
|---|---|----|----|---|---|
| x | 6 | 2  | 10 | 4 | 8 |
| y | 9 | 11 | ?  | 8 | 7 |

- (i) Estimate missing observation  
(ii) Calculate correlation coefficient.

- 7) Find correlation coefficient from the following data, [Given :  $\sqrt{3} = 1.732$ ]

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| X | 3 | 6 | 2 | 9 | 5 |
| Y | 4 | 5 | 8 | 6 | 7 |

- 8) Correlation coefficient between  $x$  and  $y$  is 0.3 and their covariance is 12. The variance of  $x$  is 9, find the standard deviation of  $y$ .



### Let's Remember

- 1) Bivariate data is the observation recorded on two variables.
- 2) Correlation is the study of mutual or joint relationship between two variables.
- 3) There are 3 types of correlation,  
i) Positive correlation ii) Negative correlation iii) No correlation.
- 4) Correlation coefficient between the variables  $x$  and  $y$  is given by  $r_{xy} = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$
- 5)  $-1 \leq r \leq 1$ .
- 6) Numerical value of correlation coefficient is invariant to the change of origin and scale.

$$\begin{aligned} 7) \text{ cov}(x, y) &= \frac{1}{n} \Sigma(x_i - \bar{x})(y_i - \bar{y}) \\ &= \frac{1}{n} \Sigma x_i y_i - \bar{x} \bar{y} \end{aligned}$$

### MISCELLANEOUS EXERCISE

- 1) Two series of  $x$  and  $y$  with 50 items each have standard deviations 4.8 and 3.5 respectively. If the sum of products of deviations of  $x$  and  $y$  series from respective arithmetic means is 420, then find the correlation coefficient between  $x$  and  $y$ .
- 2) Find the number of pairs of observations from the following data,  
 $r = 0.15$ ,  $\sigma_y = 4$ ,  $\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 12$ ,  
 $\Sigma(x_i - \bar{x})^2 = 40$ .



- 3) Given that  $r = 0.4$ ,  $\sigma_x = 3$ ,  
 $\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 108$ ,  $\Sigma(x_i - \bar{x})^2 = 900$ .  
 Find the number of pairs of observations.
- 4) Given the following information,  $\Sigma x_i^2 = 90$ ,  
 $\Sigma x_i y_i = 60$ ,  $r = 0.8$ ,  $\sigma_y = 2.5$ , where  $x_i$  and  
 $y_i$  are the deviations from their respective  
 means. Find the number of items.
- 5) A sample of 5 items is taken from the  
 production of a firm. Length and weight of  
 5 items are given below,  
 [Given :  $\sqrt{0.8823} = 0.9393$ ]

|             |   |    |    |    |    |
|-------------|---|----|----|----|----|
| Length(cm)  | 3 | 4  | 6  | 7  | 10 |
| Weight(gm.) | 9 | 11 | 14 | 15 | 16 |

Calculate correlation coefficient between  
 length and weight and interpret the result.

- 6) Calculate correlation coefficient from the  
 following data, and interpret it.

|   |    |    |   |   |   |    |    |
|---|----|----|---|---|---|----|----|
| X | 1  | 3  | 5 | 7 | 9 | 11 | 13 |
| Y | 12 | 10 | 8 | 6 | 4 | 2  | 0  |

- 7) Calculate correlation coefficient from the  
 following data and interpret it.

|   |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|
| x | 9  | 7  | 6  | 8  | 9  | 6  | 7  |
| y | 19 | 17 | 16 | 18 | 19 | 16 | 17 |

- 8) If the correlation coefficient between  $x$  and  
 $y$  is 0.8, what is the correlation coefficient  
 between i)  $2x$  and  $y$  ii)  $\frac{x}{2}$  and  $y$  iii)  $x$  and  
 $3y$  iv)  $x-5$  and  $y-3$  v)  $x+7$  and  $y+9$  vi)  
 $\frac{x-5}{7}$  and  $\frac{y-3}{8}$  ?

- 9) In the calculation of the correlation  
 coefficient between height and weight  
 of a group of students of a college, one  
 investigator took the measurements in inches  
 and pounds while the other investigator  
 took the measurements in cm. and kg. Will  
 they get the same value of the correlation  
 coefficient or different values? Justify your  
 answer.

### Activity 5.1

Calculate the correlation coefficient between  
 weight and height in Activity 4.2

### Activity 5.2

Calculate the correlation coefficient between  
 age (in years) and blood pressure from  
 Exercise 4 of Miscellaneous 4.

### Activity 5.3

Using the given data plot the points & draw  
 the scatter diagram. And identify the type of  
 correlation.

|   |   |    |    |    |    |    |    |
|---|---|----|----|----|----|----|----|
| X | 8 | 12 | 16 | 20 | 24 | 28 | 32 |
| Y | 2 | 3  | 4  | 5  | 6  | 7  | 8  |

### Activity 5.4

Select any 2 stocks and record the share  
 prices for 10 days. Draw the scatter diagram  
 of them.

